

Enhancement in spin-torque efficiency by nonuniform spin current generated within a tapered nanopillar spin valve

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We examine the effect that a spatially nonuniform spin current with a component polarized partially out of the plane has on a low saturation magnetization nanomagnet free layer. Micromagnetic simulations indicate that the spin-torque efficiency acting upon the reversing nanomagnet can be enhanced through this process, resulting in faster switching with smaller currents. In doing so, we determine that micromagnetic structure within the nanomagnets can be beneficial for reversal processes. We experimentally verify this enhancement in devices with a tapered nanopillar geometry that generates a spin current polarized partially out of plane.

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I. INTRODUCTION

The ability of a spin-polarized current pulse to rapidly reverse the orientation of a thin film nanomagnet through the transfer of spin angular momentum has been extensively studied due to possible uses in high performance magnetic random-access memory (MRAM). However, the realization of spin torque (ST) MRAM (ST-MRAM) requires that the current level for reliable and fast writing be low enough to be compatible with both scaled complementary metal-oxide-semiconductor transistors and high-performance magnetic tunnel junctions that are employed as MRAM elements.¹⁻³ Additional requirements for data retention demand that the nanomagnet have a strong enough combination of anisotropy field H_K and magnetic moment m so that there is a sufficient energy barrier U_A opposing random thermal reversal of the nanomagnet orientation.^{4,5} This poses a significant challenge, since the current for ST reversal also scales with m , making the current (density) levels for fast (<3 ns) ST writing quite high, >1 mA (>10⁷ A/cm²), in experiments to date.⁶⁻⁸

Several methods have been examined to reduce the ST reversal current I_s . One approach is to increase the spin polarization P of the incident current, but this effect begins to saturate^{9,10} once $P > 66\%$. At that point, the angular momentum transferred per electron with polarization transverse to m becomes very close to the ideal limit, neglecting spin accumulation effects that can occur in spin-valve structures.¹¹⁻¹³ By combining this approach with two reference layers bracketing the free layer, I_s can be further reduced by up to a factor of 2,^{14,15} but this still may not be sufficient to realize high speed nonvolatile ST-MRAM. Other strategies involve more complicated structures, such as injecting a highly localized spin-polarized current by the use of a nanoconstriction¹⁶ or by the use of ferromagnetic multilayers where the reference and free layers are polarized out of plane¹⁷ due to intrinsic perpendicular anisotropy. Although these approaches can reduce I_s , they require advances in magnetic materials or complicated fabrication processes such that their practicality has yet to be fully demonstrated.

Here, we discuss simulations and experimental results demonstrating an alternative means of substantially enhancing the efficiency of spin-polarized currents driving the fast reversal of thin film nanomagnets in a way that does not require materials development or multiple nanolithography

steps. This approach utilizes ferromagnetic material with a comparatively low saturation magnetization density M_S and high spin filtering properties, such as Ni₈₁Fe₁₉ alloy (Py), together with a device geometry utilizing a comparatively thick reference layer with tapered sidewalls. As a consequence of the geometry, the spin current generated by the reference layer is not uniformly polarized in the plane of the film, but instead has a component with substantial out-of-plane polarization (OPP) maximized near the ends of the major axis of the device. Micromagnetic simulations (MMSs), as discussed below, predict a substantially reduced threshold current required for magnetic reversal, and a significant enhancement in the rate at which the reversal time decreases with current above this threshold. These simulations are supported by experimental ST pulse-switching results obtained from spin-valve nanopillar device structures designed and fabricated to enhance the OPP component of the current flowing between the reference and free layers. Our study indicates that tuning the geometry of a ST device to obtain a spatially nonuniform OPP current component is an enabling technique for the realization of ST-MRAM with reliable nanosecond writing at low current-pulse amplitudes.

II. SPIN-TORQUE REVERSAL

The basics of nanomagnet reversal by spin transfer in metallic multilayers are well established.^{9,18} When a spin current generated by electrons passing through or reflecting from a ferromagnetic reference layer impinges on a nanomagnet, the component of the spin current transverse to the local moment of the nanomagnet is transferred to it with an efficiency that depends on the nanomagnet's spin filtering properties. If both the polarization of the incident spin current and the easy axis of the nanomagnet are in the plane of the film, the predominant average effect of the spin transfer is, depending on the direction of current flow, to exert either an extra damping or "antidamping" torque on the nanomagnet. In the latter case, when $I = I_c$ the spin torque initiates oscillations of the free layer magnetization. When the switching current I_s is reached, the oscillations have grown in amplitude sufficiently that the nanomagnet moment develops a net component opposite to its original easy-axis orientation, at which point the spin torque causes the nanomagnet to rapidly settle into a quiescent magnetically reversed state.

I_c can be estimated analytically by modeling the nanomagnet as uniformly polarized and by employing the standard Landau–Lifschitz–Gilbert–Slonczewski (LLGS) equation to describe the behavior of this “macrospin.” When both the reference and free layers have their equilibrium moments fully in plane, we have^{9,19,20} $I_c^{+/-} = (2e/\hbar)(\alpha/\eta^{+/-})M_sV[2\pi M_{\text{eff}} + H_{\text{eff}}]$. Here, $I_c^{+/-}$ is the critical current for the onset of dynamics when the reference and free layers are nearly parallel or antiparallel, α is the Gilbert damping parameter, e is the electron charge, M_s is the saturation magnetization of the free layer, V is the free layer volume, H_{eff} is the effective field acting on the free layer, $4\pi M_{\text{eff}}$ is its effective demagnetization field (typically $4\pi M_{\text{eff}} \gg H_{\text{eff}}$), and $\eta^{(+)}$ is the spin-torque efficiency parameter, which is ≤ 0.5 in the absence of spin accumulation effects, and varies with the alignment angle θ between the free and reference magnets. To the extent that the macrospin model approximates the true critical current for ST reversal of a nanomagnet, the pathway for reducing switching currents is clear; maximize η , and minimize α , M_s , and V . However, the constraint of thermal stability, which is typically taken as requiring $U_A = M_s H_K V / 2 \geq 40 k_B T$, where T is the device operating temperature, and materials constraints determining damping ($\alpha \geq 0.01$ for conventional MRAM materials), provide limited flexibility for optimization. One strategy, since H_K scales with both M_s of the nanomagnet and its thickness, is to use a thicker free layer composed of a lower M_s material to maintain U_A , thereby lowering I_c through a reduction in the demagnetization field $4\pi M_{\text{eff}}$ (assuming high spin-torque efficiency is maintained).

A different approach for ST switching is to use a spin current polarized entirely perpendicular to the plane of the in-plane magnetized free layer.^{21,22} In this case, the predominant effect of the spin torque is to directly force the free layer magnetization out of plane. When this effect becomes large enough relative to H_K , the nanomagnet begins to freely precess about the large out-of-plane demagnetization field. Macrospin modeling²⁰ predicts this onset to be at $I_c^{\perp} = (2e/\hbar)[M_s V / \eta(\theta = \pi/2)](H_K/2)$. Reversing the spin torque after a 90° rotation of the free layer and then terminating it at the 180° point could result in very rapid reversal (~ 100 ps), but this requires both precise timing of the current pulse and higher amplitudes than spin currents polarized in-plane, since typically $H_K > \alpha(2\pi M_{\text{eff}})$.

In this paper, we demonstrate that a significant benefit in nanosecond reversal can be achieved with a combination of both in-plane and out-of-plane polarized spin currents. By employing the macrospin approximation, it is straightforward to obtain a qualitative understanding of this effect using simulations, although to our knowledge such a combination has not been previously discussed. This involves solving the LLGS equation for a single magnetic layer with a uniform moment, where the spin-torque term used was of the form in Ref. 6, with a value of $\Lambda = 1$ for the torque asymmetry parameter to directly compare to the micromagnetic simulations discussed below. Typical material parameters were used for Py: the damping constant $\alpha = 0.014$, the $T = 0$ saturation magnetization of the free layer $M_s = 650$ emu/cm³ (determined by superconducting quantum interference device magnetometry measurements), easy-axis anisotropy field H_k

$= 150$ Oe, and spin polarization²³ $P = 0.37$. These simulations show that the reversal rate of a 5 nm thick, 45×125 nm² elliptical Py nanomagnet will be substantially enhanced if, e.g., the spin current ($P = 37\%$) has its polarization 10° out of plane, in comparison to the case of an equal current that is fully in-plane polarized (IPP). This enhancement, which does not require a precisely timed pulse, occurs because the OPP component accelerates the rate at which the macrospin moment spirals out of the plane and is somewhat similar in nature to the benefit of an applied, in-plane hard-axis magnetic field applied simultaneously with an IPP current.²⁴ This enhancement grows with the OPP in the macrospin model, but when the out-of-plane torque finally becomes large enough to overcome H_k , the effect transitions from one assisting the IPP reversal mechanism to one where the OPP current dominates, resulting in a continuous precession about the demagnetization field for as long as the current is applied. We show below that when the micromagnetic behavior of nanopillar devices and of spatially nonuniform spin currents are considered, this detrimental effect can be minimized and a small OPP component can have an even greater positive effect on short-pulse ST reversal than that indicated by the macrospin model.

III. MICROMAGNETIC SIMULATIONS OF SPIN-TORQUE REVERSAL

While macrospin modeling provides qualitative understanding, MMS give better insight into the detailed reversal behavior of nanomagnetic structures.²⁵ These micromagnetic simulations²⁶ incorporate the LLGS equation (not including a fieldlike torque term) at $T = 0$ with the same spin torque and material parameters as those used in the macrospin simulations, with the exchange constant $A = 1.3 \times 10^{-6}$ erg cm⁻¹, and the volume discretized into 2.5 nm cubes for computational purposes. Static ($I = 0$) simulations of a spin-valve structure are used to determine both the field required to cancel out the average dipole field exerted on the free layer by edge charges on the reference layer for the two layer structures and to calculate the initial micromagnetic state of the free and reference layers at the dipole field. To avoid an initial state with collinear magnetic moments in the two layers, we induce an initial in-plane misalignment ($\sim 10^\circ$) by calculating the configuration with a magnetic field along the in-plane hard axis of the ellipse. This field is turned off simultaneously with the application of the current pulse for $I \neq 0$ simulations. Dynamic ($I \neq 0$) simulations include effects from magnetic interactions between the two layers and the Oersted field due to I . Spin torque is exerted upon both layers, with the local spin polarization of the current incident upon a layer being dependent on the local magnetization vector of the second ferromagnet, i.e., the current flow was assumed to be one dimensional.^{11–13} We treat spins classically and use the simplifying assumption that spins transmit the parallel component and reflect the antiparallel component of the local magnetization perfectly, depending on the direction the electrons traverse. This assumption requires us to use a value of $\Lambda = 1$ for the asymmetry parameter¹¹ to avoid false enhancement in spin torque in one reversal direction over the

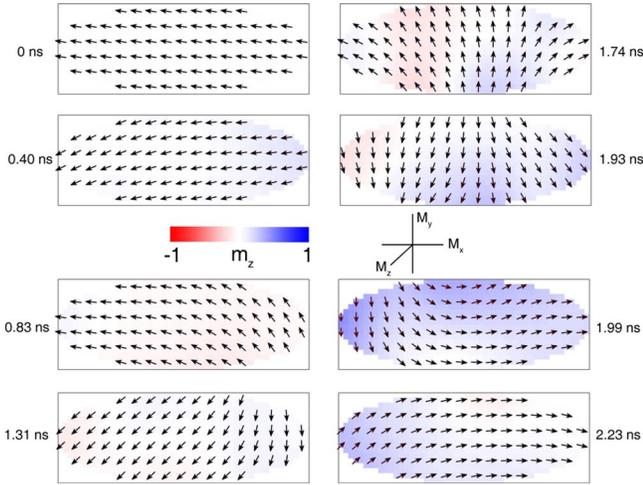


FIG. 1. (Color online) Frames of a $T=0$ micromagnetic simulation of a single 5 nm thick, 45×125 nm² elliptical nanomagnet with $I=1.5$ mA and material parameters consistent with Py. The arrows in each frame represent the local in-plane (x - y plane) magnetization of the nanomagnet, while the color scale represents the local out of plane (z axis) magnetization component. At $t=0$ ns, the average magnetization (\hat{m}_{free}) is simulated with its initial condition being initially at 170° to the polarization of the incident current (\hat{m}_p), which is uniform and in plane along the long axis of the ellipse (inset Fig. 2). Spin torque excites magnetization oscillations that evolve over time. Unlike the macrospin picture, which relies on a gradually building oscillation of the assumed uniform and rigid magnetization of the nanomagnet, we see significant magnetization oscillations begin at the edges since the demagnetization field of the magnet is $\sim 30\%$ smaller there. This manifests as a larger displacement away from the x axis at the edges of the ellipse for the times between 0 and 1.31 ns. At $t=1.74$ ns, the amplitude of the magnetization oscillations brings the magnetization approximately 90° in plane from its initial position; however, the magnetization cannot reverse due to competition from the left and right ends of the magnet. Another half precession is required ($t=1.93$ ns) to reach a state where the magnetization can fully reverse at $t=1.99$ ns. These simulations illustrate the importance the edge magnetization oscillations have on reversal behavior, growing in amplitude much more rapidly than at the center of the magnet, and eventually dragging the interior along due to exchange interactions. Thus the magnetization does not precess at all uniformly in this reversal process.

other. This choice, which neglects the spin accumulation effects that are expected to be present in spin-valve structures, still allows for a qualitative comparison of the reversal time between different device configurations.

We first consider an elliptical disk of finite thickness that has a spatially nonuniform demagnetization tensor (unlike an ellipsoid of rotation), such that the demagnetization field $4\pi M_{\text{eff}}$ significantly decreases from the center to the ends of the major axis of the disk. When properly considered by MMS, this lowers the local critical current density J_c for the onset of ST excited magnetization oscillations near the ends. Zero T simulations including the Slonczewski ST term^{11,26} (ST-MMS) reveal that, for currents slightly above I_s , ST-driven oscillations grow faster at the ends of the ellipse, resulting in a reversal process that is considerably different from uniform macrospin precession. This is indicated in Fig.

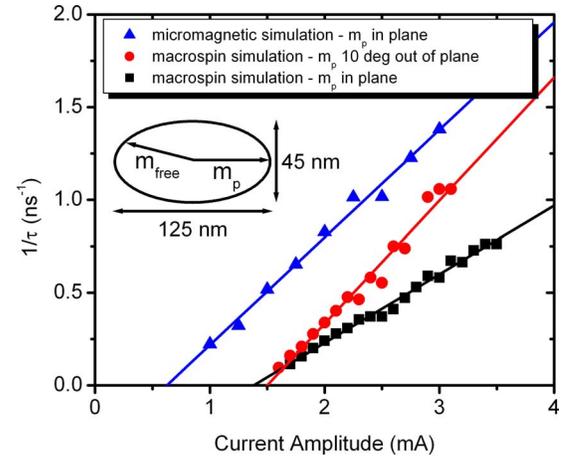


FIG. 2. (Color online) Comparison of reversal times τ for the elliptical nanomagnet discussed in Fig. 1 treated both as a macrospin and micromagnetically. From the macrospin simulations, we find that a spin current polarization (\hat{m}_p) oriented 10° out of the plane of the film can substantially enhance the magnetization reversal rates, especially for time scales on the order of 1 ns, compared to the in-plane polarization case. The large additional enhancement in reversal rate for the micromagnetic simulations indicate that the incoherent reversal mechanism shown in Fig. 1 is more efficient than coherent $T=0$ macrospin reversal. The lines are least-squares fits through the simulation results.

1, which shows the simulated micromagnetic evolution of a single 5 nm thick Py elliptical disk with 45×125 nm² cross-sectional dimensions. In Fig. 2, we plot the reversal rate for such a nanomagnet as determined by ST-MMS for a range of currents, assuming that the polarization of the incident electrons is in-plane and uniform across the nanomagnet's surface. In comparison to macrospin simulations employing the same material parameters and spin-transfer efficiency η , the micromagnetic calculation predicts a reduced critical current and a switching rate at a larger current increased by approximately a factor of 2. The result of a macrospin simulation for the case where the incident spin current is polarized 10° out of plane is also shown for comparison. While the macrospin simulation indicates that an out-of-plane polarization is effective in enhancing ST reversal in the shorter pulse regime, the micromagnetic details indicate faster reversal over the entire range of pulse widths that we have simulated. ST-MMS does indicate that the ST enhancement due to the micromagnetics of a thick, low M_s free layer is slightly lower when a typical fully patterned, spin-valve nanopillar device structure is modeled. Then, if the reference layer is assumed to be uniformly magnetized in-plane, ST-MMS predicts switching rates as shown in Fig. 3(d), with the difference from Fig. 2 being attributed to the effect of the nonuniform component of dipole field from the reference layer in suppressing magnetization oscillations at the ends of the free layer.

This detrimental effect of the dipole field can be largely countered by choosing the reference layer geometry and material so as to generate a *spatially nonuniform* spin current with a significant OPP component. Such a spin current can be obtained by using a relatively thick (~ 20 nm) low- M_s

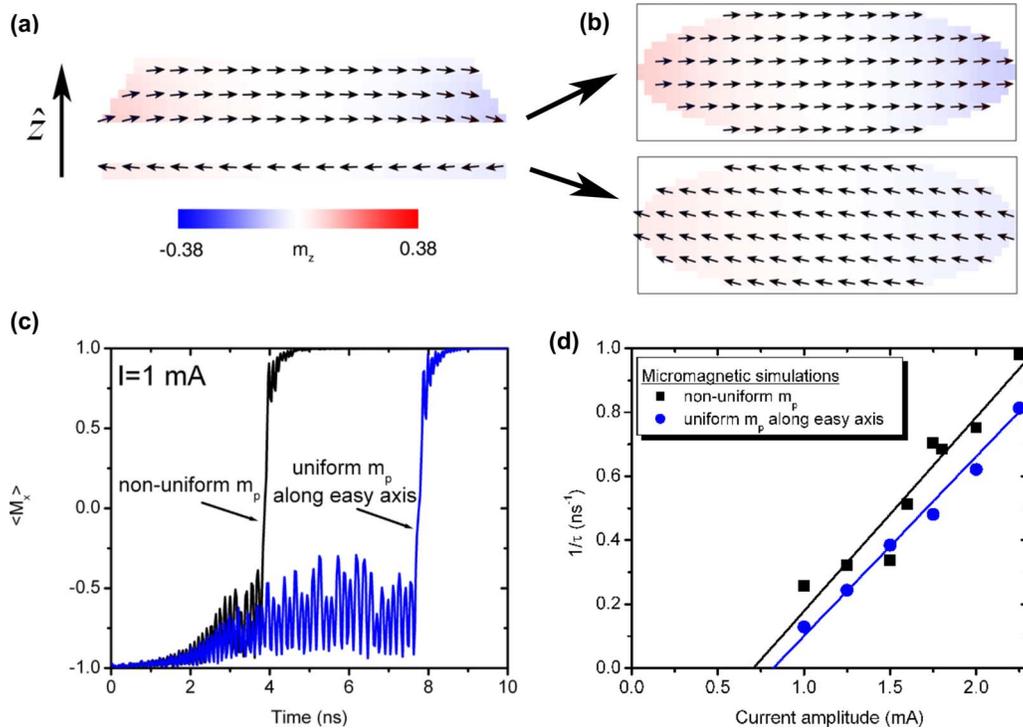


FIG. 3. (Color online) (a) $T=0$ equilibrium state of a two-layer structure with a tapered reference layer above the free layer, as calculated with MMS. (b) Misaligned ($\sim 10^\circ$) state of the adjacent reference and free layer interfaces calculated by MMS assuming the tapered device geometry and the existence of a 200 Oe in-plane hard-axis magnetic field. This misaligned state is used as the initial configuration for the dynamic simulations to avoid artifacts associated with a nearly collinear initial state. For the configuration in (b), the magnetization near the edges of the reference layer significantly curls out of plane, which generates current with a partial OPP component and enhances the magnetization oscillations at the edges of the free layer. The amplitude of these oscillations quickly grows with the assistance of this nonuniform polarization, leading to a significantly faster reversal than with a uniform in-plane polarization along the easy axis, as seen in (c), which shows the evolution of the average free layer M_x with time at 1 mA. Because the reversal process starts at the ends of the major axis of the free layer and then spreads to involve the entire nanostructure through the exchange interaction, the amplitude of M_x does not monotonically grow until the reversal point as it does in the macrospin model. (d) The rates for AP \rightarrow P reversal predicted by ST-MMS for the spatially nonuniform OPP case are enhanced compared to the results assuming a uniform, in-plane fixed-layer magnetization along the easy axis. The lines are least-squares fits through the ST-MMS results, which deviate from linear behavior due to the incoherent nature of the reversal.

reference layer so that demagnetization effects result in an out-of-plane magnetization component at the ends of the major axis of a patterned ellipse. This effect is enhanced by tapering the edges of the reference layer, which can be accomplished via directional ion beam milling during nanopillar patterning. A cross-sectional view of the $I=0$ equilibrium state of this Py-Cu-Py spin-valve structure modeled with MMS is shown in Fig. 3(a). For this structure, the magnetization cants $\sim 20^\circ$ out of plane at the ends of the interface adjacent to the free layer and gradually transitions to fully in plane near the center. Our ST-MMS calculations for magnetic reversal in this geometry include the interactions between the free and reference layers, both magnetically and by using the reference layer magnetization to determine the local current polarization acting upon the free layer, starting in the misaligned state shown in Fig. 3(b). The simulations show that the OPP component initiates large magnetization oscillations at the ends of the free layer more rapidly than with the use of a uniform IPP current for the same initial starting state, accelerating the reversal process [see Fig. 3(c)]. For reversal times in the 1–3 ns range [see Fig. 3(d)],

this enhancement is especially significant since this is the timescale over which a reduction in I_s is required for applications. Our simulations do indicate that the variation of the reversal rate with bias current in the micromagnetic results may not be as regular as that predicted by macrospin modeling, as at certain bias currents the oscillations originating at the two ends can, due to the different directions of the OPP, momentarily oppose each other and slow down the transition to the reversed state. However, experimental results, as discussed in part below, suggest that thermal effects may reduce these interactions, and overall the effect of micromagnetic structure is to significantly enhance reversal efficiency.

IV. EXPERIMENTAL DEMONSTRATION OF SPIN-TORQUE ENHANCEMENT

We confirmed these beneficial micromagnetic effects with experiments on Py-Cu-Py spin-valve nanopillar devices fabricated from thin film multilayers deposited in two different configurations. In the first, or “standard” case, the multilayer was deposited in the following sequence: 120 Cu/20 Py/12

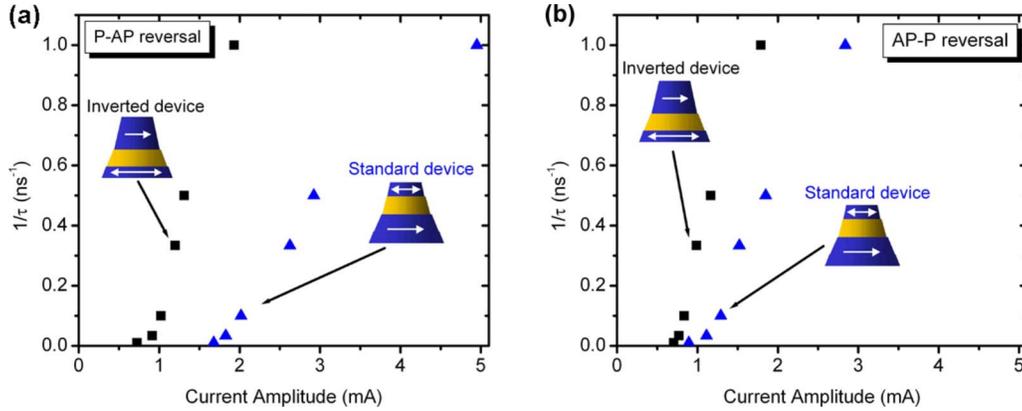


FIG. 4. (Color online) We compare reversal rate vs current for two different device structures, with the reference layer either above (inverted device) or below (standard device) the free layer. In both cases, the sidewalls were tapered during the ion milling required for nanopillar definition. The standard-structure free layer is 5.5 nm thick with a nominal of $50 \times 130 \text{ nm}^2$ elliptical area, while the inverted-structure free layer is 4.5 nm thick with an area of ~ 1.5 that of standard structure. We measured both the (a) $P \rightarrow AP$ and (b) $AP \rightarrow P$ reversal probabilities for current pulses between 1 and 100 ns long, and for a given pulse length, we define the reversal current as the value which first achieves reversal 95% of the time. A large enhancement occurs for the inverted structure, despite the larger free layer volume.

Cu/5.5 Py/2Cu/30 Pt, where Py is $\text{Ni}_{81}\text{Fe}_{19}$ and the thicknesses are in nm. For the “inverted” case, the multilayer stack was 120 Cu/4.5 Py/12 Cu/20 Py/2Cu/30 Pt, placing the reference layer of the patterned nanopillars above the free layer rather than below it. Here, ion mill characterization tests show that for the 45° mill angle used to define the nanopillars, we were able to achieve a tapered profile, which we estimate from scanning electron microscopy studies of similar ion milled structures to be approximately 30° . This estimated taper angle gives us free layer volumes which are in good agreement with extrapolated volumes determined from magnetic field properties. The nominal lateral dimensions of the elliptical nanopillar structures were $50 \times 130 \text{ nm}^2$, but sidewall tapering of the device during ion milling results in inverted samples having both larger free layers and reference layers with a substantial out-of-plane magnetization component on the side adjacent to free layer [as in Fig. 3(a)]. Due to changes in the free layer’s aspect ratio in the two different configurations, the average free layer coercive fields are smaller for the inverted devices ($47 \pm 7 \text{ Oe}$) than those for the standard devices ($218 \pm 42 \text{ Oe}$). However, since a majority of the current polarization is still in plane, I_s is dependent on $M_s \gg H_c$, so we would not expect a large change in reversal currents for this difference in coercive field.

For comparison to MMS, we performed room temperature measurements to determine ST reversal probabilities as a function of current amplitude over a range of pulse widths (1–100 ns), all of which have a significant distribution due to thermal fluctuations.^{6,27} Figure 4 plots the pulse current amplitudes I_s required to provide 95% reversal probability as a function of pulse width for a representative device of each configuration type, for the two cases where the free layer of both device configurations is reversed from a state antiparallel to the reference layer to one parallel ($AP \rightarrow P$) and vice versa ($P \rightarrow AP$). Similar results were seen in four to five devices each of standard and inverted configurations. As predicted by ST-MMS (cf. Fig. 2), the variation of the short-pulse reversal rate with I for standard devices is indeed con-

siderably more rapid than that predicted by the macrospin model when applied for the case of $P \sim 0.37$ and free layer dimensions of the standard devices. Even more notably and also in qualitative accord with ST-MMS, the inverted devices exhibit lower switching currents and a stronger variation with current amplitude than the standard devices, despite a free-layer volume estimated to be ~ 1.2 larger.

One final point to note is that we find that the asymmetry ratio of switching currents, I_c^+/I_c^- , is considerably less in the inverted vs the standard devices, ~ 1.2 vs ~ 1.6 , and in both cases considerably less than that predicted by one-dimensional spin transport analysis.^{11–13} We attribute this to a reduction in accumulated spins within the spacer layer due to the nonuniform magnetization of the reference layer. This spin accumulation would normally act to increase η^- while decreasing η^+ , leading to a strong asymmetry in switching currents. Since there is a larger out-of-plane magnetization component at the reference layer interface adjacent to the free layer in the inverted devices, spin accumulation effects will be more significantly reduced for that configuration, which is consistent with the greater symmetry in switching currents seen in the inverted devices.

V. CONSEQUENCES AND CONCLUSIONS

More extensive $T > 0$ MMS analysis and experimental studies will be required to fully quantify and optimize these micromagnetic enhancement effects, but clearly they can be quite significant. We have shown that nonuniform pathways for magnetization reversal can lead to much faster switching in spin-valve systems. By using relatively simple fabrication techniques, we can induce magnetization configurations in both magnetic layers that take advantage of these nonuniform reversal mechanisms to obtain more efficient reversal. Future development of this approach for MRAM applications would require the use of magnetic tunnel junctions, where these effects could be easily incorporated. We note that a voltage-dependent fieldlike contribution to the spin

torque that has been found to be significant in tunnel junctions²⁸ should also augment the OPP effect due to the micromagnetics of this proposed structure, leading to an even more efficient ST reversal process. Although it is quite likely that the combination of several techniques for the enhancement of spin-torque reversal will be required to finally achieve the low switching current values necessary for MRAM applications, we expect that the enhancement in the spin-torque reversal that can be achieved by the micromagnetic mechanisms discussed here will play an important role in the final spin-torque device implementation.

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